

# A Novel Drain Current $I$ – $V$ Model for MESFET

Ban-Leong Ooi, *Member, IEEE*, J. Y. Ma, and M. S. Leong, *Senior Member, IEEE*

**Abstract**—The conventional approach for modeling the dc  $I$ – $V$  characteristics of a MESFET transistor usually adopts the hyperbolic tangent dependence on  $V_{ds}$ . On the contrary, our new empirical model describes the device drain current as a polynomial of effective gate–source voltage  $V_{eff}$ . The derived model is capable of accurately model the subthreshold effect and the device current–voltage behavior at different operating regions, in particular, the device operation around the pinchoff region. Measured and modeled results of a 0.5- $\mu$ m gatelength MESFET device are compared and good agreement has been obtained. Comparisons between the proposed model, Curtice model, Chalmers model, and Parker model are also made in this paper. In addition, a single-stage class-AB amplifier was built with a commercial high-power MESFET transistor to verify the new model.

**Index Terms**—Large-signal model, MESFET, nonlinear model.

## I. INTRODUCTION

A N ESSENTIAL prerequisite for computer-aided design (CAD) software to obtain a reliable design is the existence of an accurate nonlinear model for active device. A variety of analytical models [1]–[4] have been developed to describe the operation characteristics of a MESFET. All of these models are capable of expressing the device properties with only some success in a certain region of device operation.

Among these nonlinear characteristics, the most important one is the drain–source current performance with respect to drain–source and gate–source voltages. Conventional models [1]–[4] usually assume the drain current equation as the product of the following two functions:

$$I_{ds}(V_{gs}, V_{ds}) = F_1(V_{gs}, V_{ds}) \cdot F_2(V_{gs}, V_{ds}) \quad (1)$$

where both  $F_1$  and  $F_2$  are functions of  $V_{gs}$  and  $V_{ds}$ . The first function is mainly aimed at describing the drain current variation with gate voltage. The second term, which adopts a hyperbolic function, focuses on the modeling of drain current variation with drain voltage.

In this paper, instead of using (1), a new drain current model is proposed. The drain current is now modeled as a third-order polynomial of effective gate–source voltage  $V_{eff}$ , which, in turn, is described by a rational function of  $V_{gs}$ . The model equation is unique and simple. In addition, it is very accurate in various device operation regions. In particular, the performance prediction close to pinchoff region is greatly improved.

A submicrometer wafer MESFET device and a Fujitsu FLC103WG packaged high-power MESFET transistor are adopted to verify the proposed model. A simple single-stage

class-AB amplifier was built with a Fujitsu FLC103WG high-power device to verify the new model. The simulation and measurement results of the intermodulation distortion of this amplifier are compared.

## II. NEW LARGE-SIGNAL MODEL

In this paper, the drain current characteristic assumes the following form:

$$I_{ds} = b_1 V_{ds} V_{eff}^3 + \frac{b_4 V_{ds} (b_2 + b_3 V_{ds}) V_{eff}^2}{\sqrt{(1 + g V_{gst})^2 + V_{ds}^2 (b_2 + b_3 V_{ds})^2}} + \frac{b_5 V_{ds} (b_2 + b_3 V_{ds}) V_{eff}}{\sqrt{(1 + g V_{gst})^2 + V_{ds}^2 (b_2 + b_3 V_{ds})^2}} \quad (2)$$

where

$$\begin{aligned} V_{gst} &= V_{gs} - V_{TO} + \gamma V_{ds} \\ V_{eff3} &= 0.5 \left( V_{gst} (1 + c_{pin}) + \sqrt{V_{gst}^2 + V_{ST}^2 (1 - c_{pin})} \right) \\ V_{eff} &= V_{ST} (1 + M_{VST} V_{ds}) \ln \left( 1 + e^{V_{eff3} / (V_{ST} (1 + M_{VST} V_{ds}))} \right). \end{aligned} \quad (3)$$

$V_{TO}$  is the pinchoff voltage,  $\gamma$ ,  $b_1$ ,  $b_2$ ,  $b_3$ ,  $b_4$ ,  $b_5$ ,  $g$ ,  $V_{ST}$ ,  $M_{VST}$ , and  $c_{pin}$  are the model parameters that are introduced to improve the subthreshold and pinchoff regions and, finally,  $V_{gs}$  and  $V_{ds}$  are the intrinsic terminal voltages.

Applying a large negative gate potential to an FET never succeeds in completely cutting off the drain current, as the channel mobile carrier density declines less rapidly than that predicted from the abrupt depletion approximation. Near pinchoff, the current diminishes exponentially with gate potential and will increase when gate-drain breakdown occurs [6]–[8]. The transformation of  $V_{gs}$  into effective gate–source voltage  $V_{eff}$  through (2) accurately describes the device operation around the pinchoff region. This transformation is well behaved and infinitely differentiable. Thus, it serves to be a good representation for intermodulation characteristics.

## III. MODEL PARAMETER EXTRACTION

A  $2 \times 150 \mu$ m submicrometer gatelength MESFET device (wafer device) and a Fujitsu FLC103WG packaged high-power MESFET transistor are used to verify the new model. The  $S$ -parameter data are measured at a multibias condition. The small-signal equivalent-circuit models are extracted under a multibias condition using the cold FET method combined with a multiplane data-fitting approach [9]. All the parasitic element values are kept constant in the large-signal model. The extracted parasitic element values are listed in Tables I and II, respectively,

Manuscript received February 21, 2000.

The authors are with the Electrical and Computer Engineering Department, National University of Singapore, Singapore 119260 (e-mail: eleoobl@nus.edu.sg).

Publisher Item Identifier S 0018-9480(02)03036-3.

TABLE I  
PARASITIC ELEMENT VALUES FOR WAFER DEVICE

$C_{pg}(\text{fF})$	$C_{pd}(\text{fF})$	$L_g(\text{pH})$	$L_d(\text{pH})$
32.9	30.1	155.4	160.6
$L_s(\text{pH})$	$R_s(\Omega)$	$R_g(\Omega)$	$R_d(\Omega)$
3.0	2.1	5.9	4.3

TABLE II  
PARASITIC ELEMENT VALUES FOR FUJITSU FLC103WG

$C_{pg}(\text{pF})$	$C_{pd}(\text{pF})$	$L_g(\text{nH})$	$L_d(\text{nH})$
1.31	0.436	1.49	1.29
$L_s(\text{pH})$	$R_s(\Omega)$	$R_g(\Omega)$	$R_d(\Omega)$
59.5	0.99	1.53	1.96

TABLE III  
MODEL PARAMETERS FOR WAFER DEVICE

$V_{TO}(\text{V})$	$\gamma$	$V_{ST}$	$b_1$	$b_2$	$b_3$
-1.21	0.0358	0.103	-0.71	2.783	4.235
$b_4$	$b_5$	$g$	$M_{VST}$	$cpin$	
14.31	23.96	0.196	0.162	1.562	

TABLE IV  
MODEL PARAMETERS FOR THE FUJITSU FLC103WG

$V_{TO}(\text{V})$	$\gamma$	$V_{ST}$	$b_1$	$b_2$	$b_3$
-2.28	9.16e-3	0.436	-4.85	0.78	0.241
$b_4$	$b_5$	$g$	$M_{VST}$	$cpin$	
102.4	221.86	-0.136	-0.068	4.87	

for the two devices. The large-signal model parameters are extracted from the drain current  $I$ - $V$  data at the intrinsic device plane and are listed in Tables III and IV, respectively, for the two devices. All the parameter extractions are performed by in-house developed software running under MATLAB. A simplex algorithm is used for the optimization.

#### IV. MODELING RESULTS AND DISCUSSIONS

The model parameters for the  $2 \times 150 \mu\text{m}$  submicrometer gatelength on-wafer MESFET device are extracted for the Curtice model [1], Chalmers model [2], Parker model [5], and the new model. These results are clearly plotted in Fig. 1 together with the measured data.

As observed from Fig. 1, the fitting error for Curtice model [1] is quite significant in the linear, knee, and saturation regions, especially as the drain current is reduced. It also has a conditional cutoff in the pinchoff region. The Chalmers model [2]

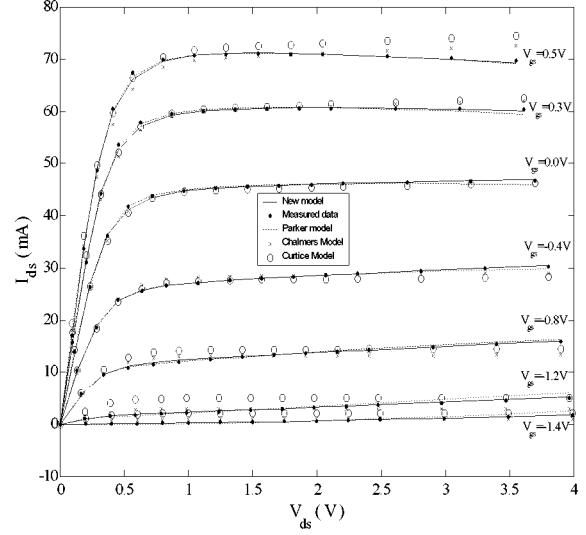


Fig. 1. Comparison of measured and modeled drain current characteristics of the new model, Parker model, Chalmers model, and Curtice model (wafer device).

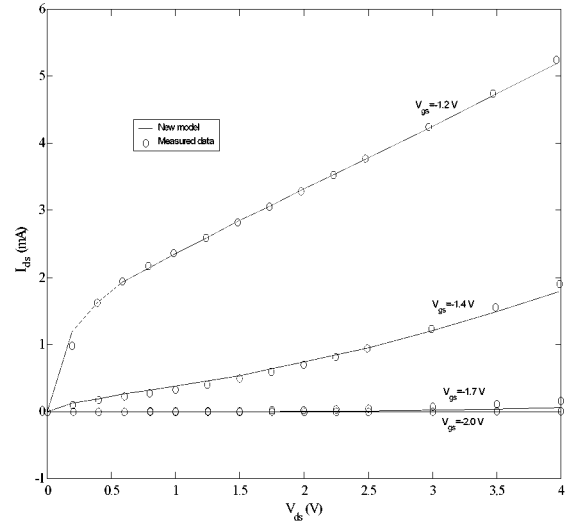


Fig. 2. Comparison of measured and proposed drain current characteristics around pinchoff region ( $V_{pinchoff} = -1.21 \text{ V}$ , wafer device).

offers an improvement over the Curtice model, but the fitting of the Chalmers model in the knee and saturation regions and for small drain current is still poor. Both the Parker model [5] and proposed new model give very accurate fitting results over various device operation regions. The small negative  $I_{ds}$ - $V_{ds}$  slope for large  $I_{ds}$  is well described by our model. The modeled drain current goes smoothly to zero when  $V_{gs}$  approaches or drops below pinchoff. Our model also gives an accurate subthreshold modeling, as depicted in Fig. 2.

Fig. 3 gives the comparison between the measured and simulated  $I_{ds}$ - $V_{gs}$  and  $g_m$ - $V_{gs}$  characteristics of the same wafer device. The measured and simulated  $g_m$  results near the pinchoff region of the same device are presented in Fig. 4. Figs. 5

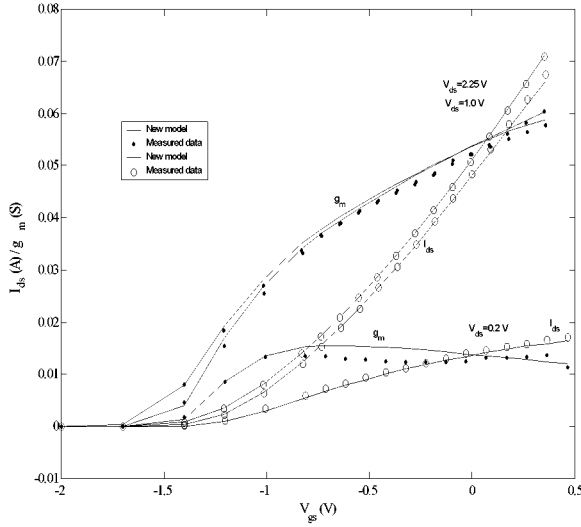


Fig. 3. Comparison of measured and simulated  $I_{ds}$ - $V_{gs}$  and  $g_m$ - $V_{gs}$  characteristic based on the new model (wafer device).

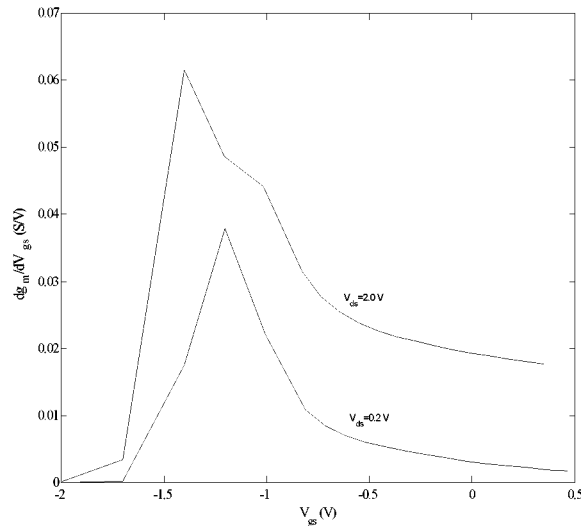


Fig. 4. Comparison of measured and simulated  $g_m$  characteristic close to pinchoff based on the new model (wafer device).

and 6 give the simulated  $\partial g_m / \partial V_{gs}$  versus  $V_{gs}$  and  $\partial^2 g_m / \partial^2 V_{gs}$  versus  $V_{gs}$  characteristics, respectively.

The maximum fitting error and the rms error of all models are listed in Table V for comparison. The calculation is made for five bias levels for  $V_{gs}$ , while  $V_{ds}$  changes from 0.5 to 4.0 V (on-wafer device). As noted from Table V, both the maximum fitting error and the rms error are greatly reduced for the new model, as compared to the Curtice and Chalmers models. The maximum fitting error and rms error for both the Parker and new models are all very small. However, near the pinchoff condition ( $V_{gs} = -1.2$  V,  $V_{pinchoff} = -1.2$ – $-1.21$  V), the new model outperforms the Parker model. The newly proposed model contains more model parameters than the Curtice [1] and Chalmers models [2]. However, from the parameter-extraction procedure, there is no significant increase in simulation time required for

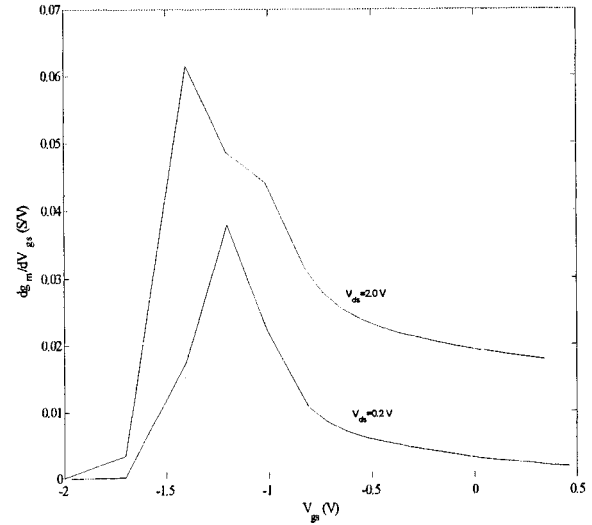


Fig. 5. Simulated  $\partial g_m / \partial V_{gs}$  versus  $V_{gs}$  characteristic.

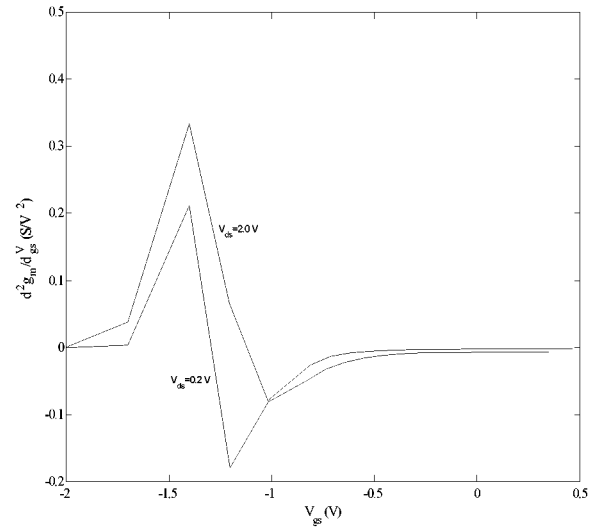


Fig. 6. Simulated  $\partial^2 g_m / \partial^2 V_{gs}$  versus  $V_{gs}$  characteristic.

TABLE V  
COMPARISON OF THE MAXIMUM FITTING ERROR AND RMS ERROR OF THE NEW MODEL WITH THE CURTICE, CHALMERS, AND PARKER MODELS (WAFFER DEVICE)

Models		New Model	Parker Model	Curtice Model	Chalmers Model
$V_{gs} = 0.5$ V ( $V_{ds} = 0.5$ – $4.0$ V)	Max. Err. (%)	1.90	1.17	6.77	5.19
	RMS Err. (%)	0.78	0.55	3.26	2.71
$V_{gs} = 0.0$ V ( $V_{ds} = 0.5$ – $4.0$ V)	Max. Err. (%)	1.54	1.81	2.81	2.70
	RMS Err. (%)	0.50	0.72	1.48	1.08
$V_{gs} = -0.5$ V ( $V_{ds} = 0.5$ – $4.0$ V)	Max. Err. (%)	0.56	1.46	7.73	6.13
	RMS Err. (%)	0.26	0.52	3.91	3.83
$V_{gs} = -0.8$ V ( $V_{ds} = 0.5$ – $4.0$ V)	Max. Err. (%)	2.43	1.82	18.83	16.75
	RMS Err. (%)	1.20	1.00	11.14	8.78
$V_{gs} = -1.2$ V ( $V_{ds} = 0.5$ – $4.0$ V)	Max. Err. (%)	1.31	17.89	146.8	45.47
	RMS Err. (%)	0.75	10.13	82.6	27.39

the new model. This is because the new model only uses simple functions instead of a hyperbolic-tangent-type function, which

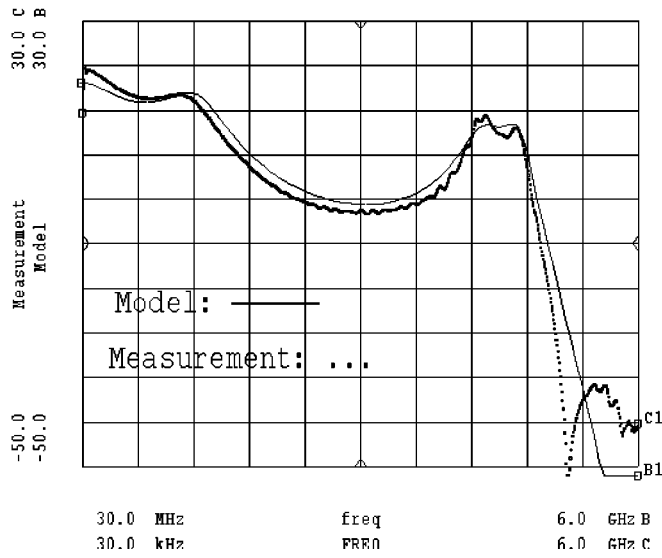


Fig. 7. Comparison of measured and simulated  $S_{21}$  of the amplifier.

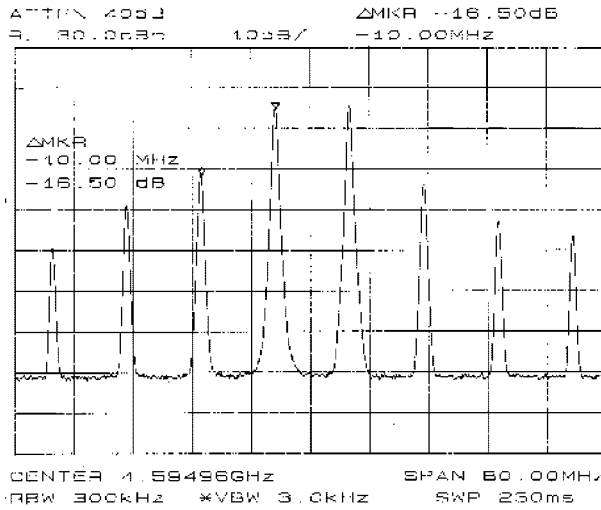


Fig. 8. Measured third-order intermodulation distortion of the amplifier ( $P_{in} = 10$  dBm).

requires more simulation time and, most importantly, the model is continuous. The proposed model gives a comparable performance to the Parker model [5] and the number of model parameters is one less than the Parker model. The new model can be easily implemented in CAD software and could be very useful in microwave circuit simulation.

#### V. AMPLIFIER DESIGN RESULT WITH THE NEW MODEL

A single-stage class-AB amplifier is designed and fabricated using Fujitsu FLC103WG to verify the performance of the new model. Good agreement was obtained. The amplifier is biased at  $V_{gs} = -1.8$  V and  $V_{ds} = 6.5$  V. The designed amplifier operates from 4.2 to 4.7 GHz with a gain of 10 dB. Both the  $S$ -parameters and third-order intermodulation distortions are measured and compared. The two-tone input signals are 4.5 and 4.51 GHz, respectively, and the input power is 10 dBm.

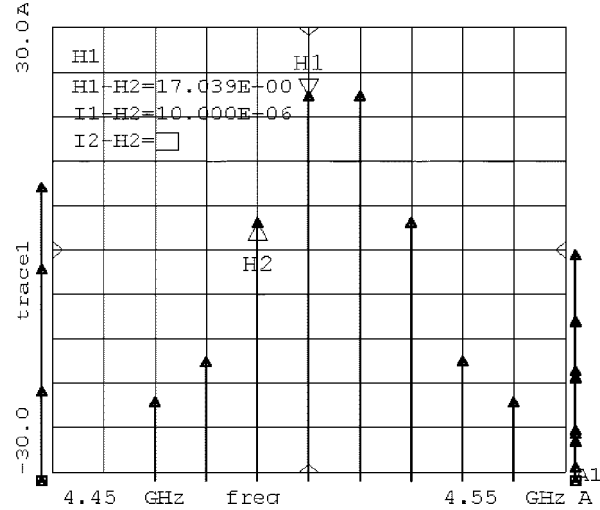


Fig. 9. Simulated third-order intermodulation distortion of the amplifier ( $P_{in} = 10$  dBm).

Fig. 7 shows the measured and simulated  $S_{21}$  performance of the amplifier. Figs. 8 and 9 are the measured and simulated third-order intermodulation distortions, respectively. The simulated response and measured performance are in good accordance.

#### VI. CONCLUSIONS

An accurate large-signal model for GaAs MESFET has been proposed in this paper. The model is capable of accurately representing the actual device characteristics over an extended range of operation conditions. Model performance near the pinchoff region is greatly improved through the use of a special transformation for  $V_{gs}$ . Moreover, the model and its derivatives are continuous, which gives a smooth transition to different operation regions. The model equations only adopt simple functions, thus, the parameter extraction is simple. It can be a useful tool for modern communication and microwave circuits design.

#### REFERENCES

- [1] W. R. Curtice, "GaAs MESFET modeling and nonlinear CAD," *IEEE Trans. Microwave Theory Tech.*, vol. 36, pp. 220–230, Feb. 1988.
- [2] I. Angelov, H. Zirath, and N. Rorsman, "A new empirical nonlinear model for HEMT devices," in *IEEE MTT-S Int. Microwave Symp. Dig.*, 1992, pp. 1583–1586.
- [3] H. Statz, P. Newman, I. W. Smith, R. A. Pucel, and H. A. Haus, "GaAs FET device and circuit simulation in SPICE," *IEEE Trans. Electron Devices*, vol. ED-34, pp. 160–169, Feb. 1987.
- [4] V. I. Cocjaru and T. J. Brazil, "A scalable general-purpose model for microwave FET's including DC/AC dispersion effects," *IEEE Trans. Microwave Theory Tech.*, vol. 45, pp. 2248–2255, Dec. 1997.
- [5] A. E. Parker and D. J. Skellern, "A realistic large-signal MESFET model for SPICE," *IEEE Trans. Microwave Theory Tech.*, vol. 45, pp. 1563–1571, Sept. 1997.
- [6] *TriQuint Semiconductor Reference Manual*, TriQuint, Hillsboro, OR.
- [7] K. De Vivek and J. D. Meindl, "Three-region analytical model for MESFET's in low-voltage digital circuits," *IEEE J. Solid-State Circuits*, vol. 26, pp. 850–855, June 1991.
- [8] M. D. Godfrey, "CMOS device modeling for subthreshold circuits," *IEEE Trans. Circuits Syst. II*, vol. 39, pp. 532–539, Aug. 1992.
- [9] F. Lin and G. Kompas, "FET model parameter extraction based on optimization with multipane data-fitting and bidirectional search—A new concept," *IEEE Trans. Microwave Theory Tech.*, vol. 42, pp. 1114–1121, July 1994.



**Ban-Leong Ooi** (M'92) received the B.Eng. and Ph.D. degree from the National University of Singapore, Singapore, in 1992 and 1997, respectively.

He is currently an Assistant Professor of Electrical and Computer Engineering, National University of Singapore. His main research interests include active antennas, microwave semiconductor device modeling and characterization, microwave and millimeter-wave circuits, and electromagnetic numerical methods.

Dr. Ooi served as the Singapore IEEE Microwave Theory and Techniques (MTT)/Electromagnetic Compatibility (EMC)/Antennas and Propagation (AP) Chapter secretary in 2000 and 2001. He was actively involved in organizing the 1999 Asia-Pacific Microwave Conference, Singapore, and served as the publication chairman for the 1999 Asia-Pacific Microwave Conference, Singapore. He was a recipient of the 1993 URSI Young Scientist Award.

**J. Y. Ma**, photograph and biography not available at time of publication.

**M. S. Leong** (M'75–SM'98), photograph and biography not available at time of publication.